## Supplemental Material

## Conditions When the Parameter $\boldsymbol{f}$ is lose to 1



Fig. 3

Fig. 3 Legend
Factor $f=\left\{\frac{z_{\alpha} \sqrt{2 \overline{p q}}+z_{\beta} \sqrt{p_{e}\left(1-p_{e}\right)+p_{c}\left(1-p_{c}\right)}}{z_{\alpha} \sqrt{2 \bar{p}_{T} \bar{q}_{T}}+z_{\beta} \sqrt{p_{e}^{T}\left(1-p_{e}^{T}\right)+p_{c}\left(1-p_{c}\right)}} \frac{1+\sqrt{1+2 w}}{1+\sqrt{1+2 w_{T}}}\right\}^{2}$ intervening in the relative efficiency of the untargeted and targeted designs with regard to number of randomized patients, $n / n^{T}=\left[\frac{\delta_{1}}{\gamma \delta_{0}+(1-\gamma) \delta_{1}}\right]^{2} f$, with $w$ and $w_{T}$ respectively defined by $w=\frac{\left(\gamma \delta_{0}+(1-\gamma) \delta_{1}\right)}{\left(z_{\alpha}+z_{\beta}\right)^{2} \overline{p q}}$ and $w_{T}=\frac{\delta_{1}}{\left(z_{\alpha}+z_{\beta}\right)^{2} \bar{p}_{T} \bar{q}_{T}} \cdot \gamma$ is the proportion of R- patients . $p_{c}$ denotes the response probability in control group and is assumed to be the same for $\mathrm{R}-$ and $\mathrm{R}+$ patients. The response probability in the treatment group is $p_{c}+\delta_{0}$ and $p_{c}+\delta_{1}$ for the R - and $\mathrm{R}+$ patients respectively. The response probability $p_{e}$ for the experimental treatment group in the untargeted design is a weighted average of $p_{c}+\delta_{0}$ and $p_{c}+\delta_{1}$ with weights $\gamma$ and (1- $\gamma$ ) respectively. The response probability in the experimental group in the targeted design is $p_{e}^{T}=p_{c}+\delta_{1}$. $\bar{p}=\left(p_{e}+p_{c}\right) / 2, \bar{q}=1-\bar{p}$ and $\bar{p}_{T}=\left(p_{e}^{T}+p_{c}\right) / 2, \bar{q}_{T}=1-\bar{p}_{T}$. The constants $z_{\alpha}$ and $z_{\beta}$ denote the $100 \alpha$ and $100 \beta$ percentiles of the standard normal distribution. The horizontal axis represents the proportion of patients who express the target and are expected to be responsive to the new treatment.

## Case 0: No Treatment effect

## for R - patients

$0: \delta_{0}=0, \delta_{1}=0.2, p_{c}=0.1$
$\times: \delta_{0}=0, \delta_{1}=0.4, p_{c}=0.1$
$+: \delta_{0}=0, \delta_{1}=0.2, p_{c}=0.5$
米: $\delta_{0}=0, \delta_{1}=0.4, p_{c}=0.5$

Case 1: Treatment effect for $R$ - patients is half as large as that for $\mathrm{R}+$ patients

$$
\begin{array}{r}
\nabla: \delta_{0}=0.1, \delta_{1}=0.2, p_{c}=0.1 \\
\text { 娒: }=0.2, \delta_{1}=0.4, p_{c}=0.1 \\
\square: \delta_{0}=0.1, \delta_{1}=0.2, p_{c}=0.5 \\
--: \delta_{0}=0.2, \delta_{1}=0.4, p_{c}=0.5
\end{array}
$$

## Assay Imprecision

Let R be a binary indicator of true tumor status; $\mathrm{R}=1$ for $\mathrm{R}+$ and $\mathrm{R}=0$ for R -.
Let A be a binary indicator of assay result; $\mathrm{A}=1$ for $\mathrm{R}+$ and $\mathrm{A}=0$ for R -.
Let Resp denote binary response; Resp=1 for response and Resp=0 for no response.
Let T denote the treatment group; $\mathrm{T}=\mathrm{c}$ for control and e for the experimental treatment.

In the paper we have assumed that
$\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{R}=0, \mathrm{~T}=\mathrm{c}\}=\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{R}=1, \mathrm{~T}=\mathrm{c}\}$.
That is, the $\mathrm{R}-$ and $\mathrm{R}+$ patients on the control treatment have the same probability of response. Consequently, it is easy to show that
$\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{c}, \mathrm{A}=0\}=\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{c}, \mathrm{A}=1\}=\mathrm{p}_{\mathrm{c}} . \quad(\mathrm{A} 1)$

$$
\begin{align*}
\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{e}, \mathrm{~A}=0\}= & \operatorname{Prob}\{\operatorname{Resp}=1, \mathrm{R}=0 \mid \mathrm{T}=\mathrm{e}, \mathrm{~A}=0\}+\operatorname{Prob}\{\operatorname{Resp}=1, \mathrm{R}=0 \mid \mathrm{T}=\mathrm{e}, \mathrm{~A}=0\} \\
= & \operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{e}, \mathrm{R}=0\} * \operatorname{Prob}\{\mathrm{R}=0 \mid \mathrm{A}=0\} \\
& +\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{e}, \mathrm{R}=1\} * \operatorname{Prob}\{\mathrm{R}=1 \mid \mathrm{A}=0\} . \\
= & \left(\mathrm{p}_{\mathrm{c}}+\delta_{0}\right)^{*} \mathrm{NPV}+\left(\mathrm{p}_{\mathrm{c}}+\delta_{1}\right)(1-\mathrm{NPV}) \\
= & \mathrm{p}_{\mathrm{c}}+\delta_{0} * \mathrm{NPV}+\delta_{1} *(1-\mathrm{NPV}) \tag{A2}
\end{align*}
$$

Where NPV denotes the negative predictive value of the assay.
Subtracting (A1) from (A2), the treatment effect for assay negative patients is
Treatment effect for assay negative patients $=\delta_{0} * \mathrm{NPV}+\delta_{1}{ }^{*}(1-\mathrm{NPV})$.

The quantity $\delta_{0}$ is the treatment effect for R- patients. If that is zero, then the treatment effect for assay negative patients is $\delta_{1} *(1-\mathrm{NPV})$ as indicated in the manuscript.

Similar to the derivation of (A1) and (A2) we can show that:
$\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{c}, \mathrm{A}=1\}=\mathrm{p}_{\mathrm{c}}$
and
$\operatorname{Prob}\{\operatorname{Resp}=1 \mid T=e, A=1\}=\operatorname{Prob}\{\operatorname{Resp}=1 \mid T=\mathrm{e}, \mathrm{R}=0\} * \operatorname{Prob}\{\mathrm{R}=0 \mid \mathrm{A}=1\}$ $+\operatorname{Prob}\{\operatorname{Resp}=1 \mid \mathrm{T}=\mathrm{e}, \mathrm{R}=1\} * \operatorname{Prob}\{\mathrm{R}=1 \mid \mathrm{A}=1\}$
$=\left(\mathrm{p}_{\mathrm{c}}+\delta_{0}\right) *(1-\mathrm{PPV})+\left(\mathrm{p}_{\mathrm{c}}+\delta_{1}\right)$ PPV
$=\mathrm{p}_{\mathrm{c}}+\delta_{0} *(1-\mathrm{PPV})+\delta_{1} * \mathrm{PPV}$.

Consequently, the treatment effect for assay positive patients is $\delta_{0} *(1-\mathrm{PPV})+\delta_{1} * \mathrm{PPV}$ which equals $\delta_{1} * \mathrm{PPV}$ when the treatment effect is limited to $\mathrm{R}+$ patients.

